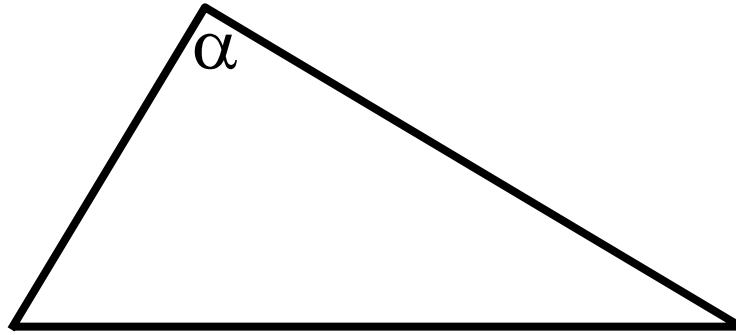


CP Violation in $B \rightarrow \rho\rho$ and Measurement of the Unitarity Triangle Angle α

CKM Workshop 2005 San Diego, CA




Adrian Bevan

Talk Overview

- Physics Motivation
 - $B \rightarrow VV$ decays (quick reminder)
 - CP Violation (v. quick reminder)
 - Isospin analysis (even quicker reminder)

- Results

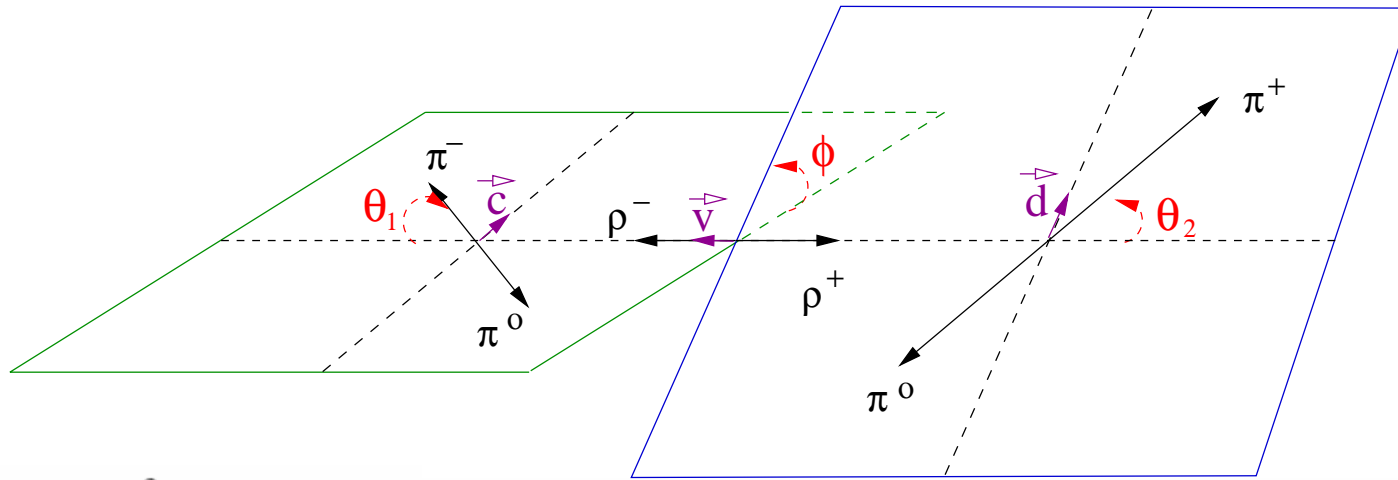
- $\rho^0\rho^0$ Result from ICHEP (210fb^{-1})
 -  new! $\rho^+\rho^-$ (210fb^{-1})
 - a few words on $\rho^+\rho^0$

- Impact on the Unitarity Triangle

- Conclusions

$B \rightarrow \rho\rho$

- ➔ VV final state
- ➔ $L=0,1,2$ partial wave components – need angular analysis to determine CP content of decay
- ➔ $\rho\rho$ is almost 100% longitudinally polarised ($f_L \sim 1$)



$$\frac{d^2\Gamma}{\Gamma d \cos \theta_1 d \cos \theta_2} = \frac{9}{4} \left(\underbrace{f_L \cos^2 \theta_1 \cos^2 \theta_2}_{\text{Longitudinal}} + \frac{1}{4} \underbrace{(1 - f_L) \sin^2 \theta_1 \sin^2 \theta_2}_{\text{Transverse}} \right)$$

Longitudinal
(CP even)
SLong & CLong

Transverse
(Mixed CP state)
Set $S_{\text{Tran}} = C_{\text{Tran}} = 0$
& vary for systematics

Like $\pi\pi$ etc., analyse time evolution of $B^0\bar{B}^0$ system

(assume $\Delta\Gamma=0$):

$$f(B^0 / \bar{B}^0_{phys} \rightarrow f / \bar{f}, \Delta t) =$$

$$\frac{\Gamma}{4} e^{-\Gamma|\Delta t|} \left[1 + \eta S \sin(\Delta m_d \Delta t) - \eta C \cos(\Delta m_d \Delta t) \right]$$

$\eta = +1(-1)$ for $B^0 (\bar{B}^0)$

Indirect CP violation $\Rightarrow S \neq 0$

Direct CP violation $\Rightarrow C \neq 0$

$$\lambda_{f_{CP}} = \frac{q}{p} \cdot \frac{\bar{A}_{f_{CP}}}{A_{f_{CP}}}$$

$$S_{f_{CP}} = \frac{2 \operatorname{Im} \lambda_{f_{CP}}}{1 + |\lambda_{f_{CP}}|^2}$$

$$C_{f_{CP}} = \frac{1 - |\lambda_{f_{CP}}|^2}{1 + |\lambda_{f_{CP}}|^2}$$

$$C = -A_{CP}$$

BaBar : Belle

Also need to worry about: tagging dilution
: resolution function

But it's a bit more complicated for $\rho\rho$...

➔ In general want to do a time dependent angular analysis (D^*D^*).

➔ As $f_L \sim 1$, most information is in a single CP even amplitude.

➔ Δt dependence is:

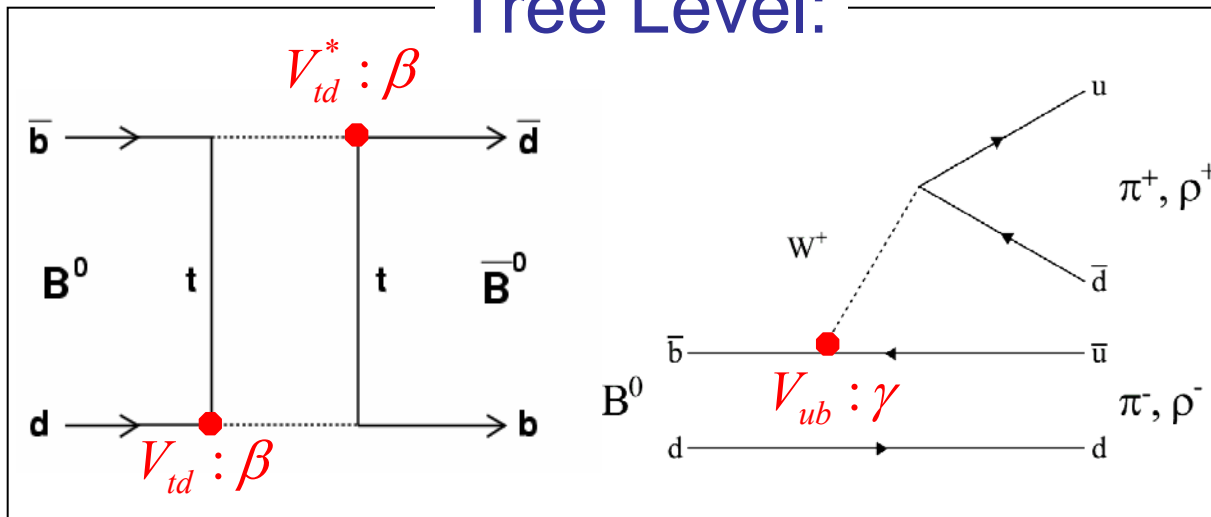
$$P_{LONG} \propto \frac{\Gamma}{4} e^{-\Gamma|\Delta t|} \left[1 + \eta S_{LONG} \sin(\Delta m_d \Delta t) - \eta C_{LONG} \cos(\Delta m_d \Delta t) \right]$$
$$P_{TRAN} \propto \frac{\Gamma}{4} e^{-\Gamma|\Delta t|} \left[1 + \eta S_{TRAN} \sin(\Delta m_d \Delta t) - \eta C_{TRAN} \cos(\Delta m_d \Delta t) \right]$$

➔ Don't care about disentangling CP admixture of the transverse polarisation into CP eigen states.

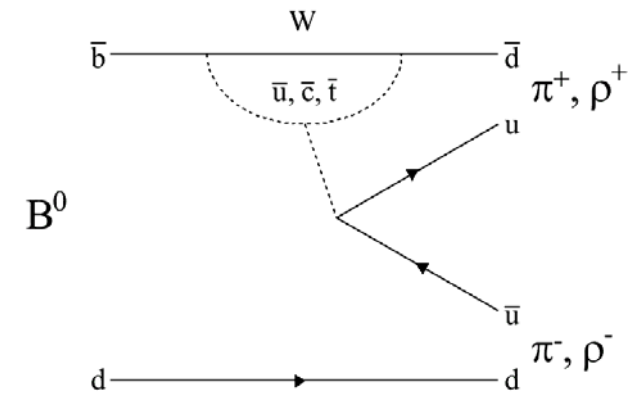
➔ So as there are very few transverse events
just set $S_{TRAN} = C_{TRAN} = 0$ in fit to data
vary between ± 1 when evaluating systematic error

CP Violation in $B^0 \rightarrow \rho^+ \rho^-$

Tree Level:



+Loops (penguins)



$$C_{\rho\rho} = 0$$

$$S_{\rho\rho} = \sin(2\alpha)$$



$$C_{\rho\rho} \propto \sin(\delta)$$

$$S_{\rho\rho} = \sqrt{1 - C_{\rho\rho}^2} \sin(2\alpha_{\text{eff}})$$

$$\delta = \delta_P - \delta_T$$

→ Same Physics as $\pi\pi/\rho\pi$

→ measure α_{eff}

→ need to bound $|\alpha_{\text{eff}} - \alpha|$ (shift from loops)

Isospin Analysis

➔ Bounds $\alpha_{\text{eff}} = \alpha$

➔ SU(2) relates different $\rho\rho$ final states
⇒ triangles for $\rho\rho$

Gronau-London: PRL **65**, 3381 (1990)

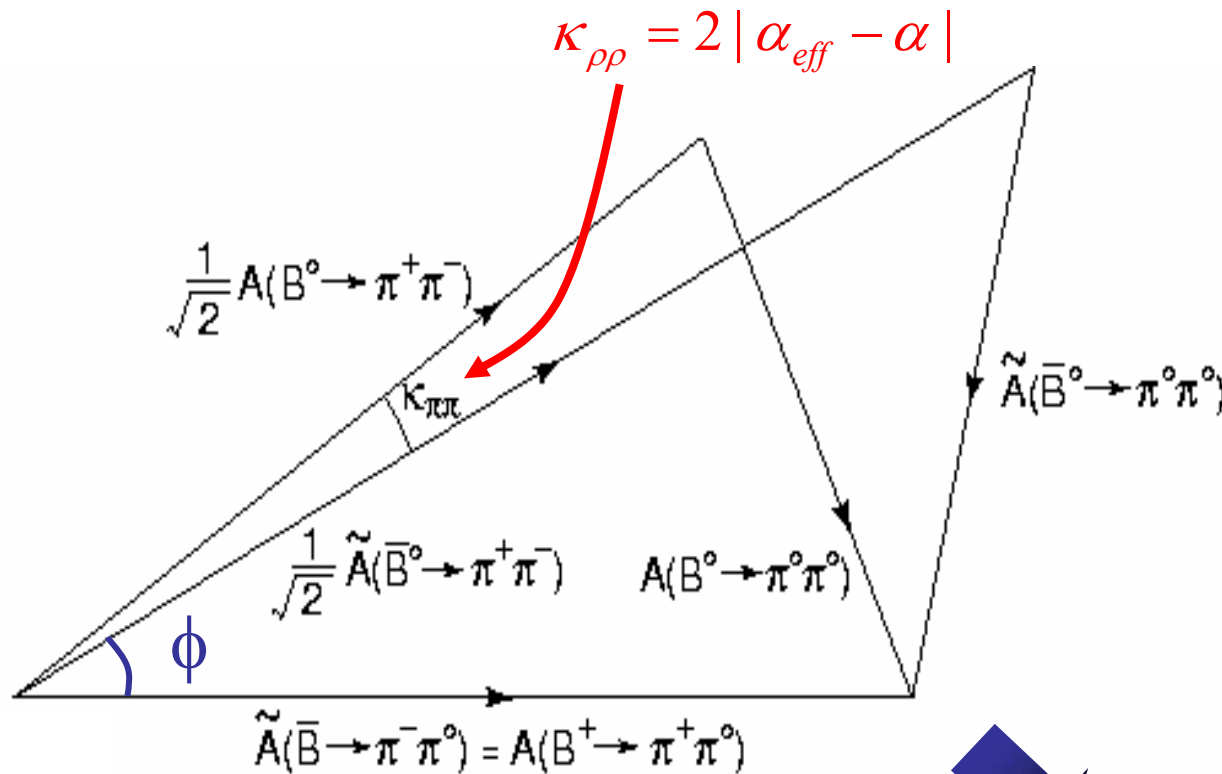
$$\frac{1}{\sqrt{2}} A_{Long}^{+-} + A_{Long}^{00} = A_{Long}^{+0}$$

$$\frac{1}{\sqrt{2}} \overline{A}_{Long}^{--} + \overline{A}_{Long}^{00} = \overline{A}_{Long}^{--0}$$

similar relations for each transversity amplitude
⇒ only care about longitudinal events as $f_L \sim 1$

➔ So if $A^{00} = 0$, we would expect $|A^{+-}|^2 = 2|A^{+0}|^2$

Isospin Analysis/determination of α



For $\rho\rho$ we require:

$$A(B^0 \rightarrow \rho^+ \rho^-) + C.C.$$

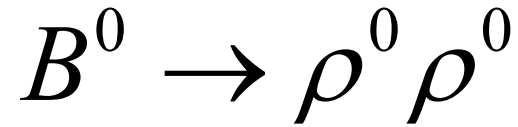
$$A(B^0 \rightarrow \rho^0 \rho^0) + C.C.$$

$$A(B^+ \rightarrow \rho^+ \rho^0) + C.C.$$

$$S_{\rho^+ \rho^-}$$

$$+ \text{Polarization: } f_L^{+-}, f_L^{+0}, f_L^{00}$$

$$\alpha_{\text{eff}} = \frac{1}{2} \arcsin \left(\frac{S_{+-}}{\sqrt{1 - C_{+-}^2}} \right) \rightarrow \alpha$$



(227e6 B Pairs)

→ Limiting factor in the $\rho\rho$ isospin analysis

→ First result published in PRL **91**, 171802 (2003)

→ $BF(B^0 \rightarrow \rho^0 \rho^0) < 1.1 \times 10^{-6}$ (90% CL)

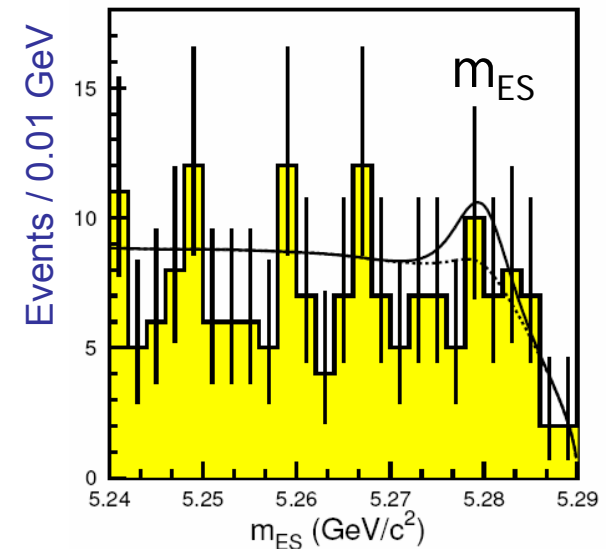
$$N_{\text{signal}} = 33_{-20}^{+22} (\text{stat})$$

→ ML fit using 8 inputs:

$$m_{ES}, \Delta E, \text{tagging}, \\ m_{\pi^+\pi^-}, \cos\theta_H, \text{MVA} \\ \times 2$$

→ Dominant Systematics:

- $a_1\pi$ interference: ± 7.5 events
- PDF variations: ± 6 events
- B bkgd: ± 5.8 events



hep-ex/0412067 (accepted for publication)

Previous $\rho^+\rho^-$ results from BaBar

- Runs 1+2 (results published in PRL, PRD):

$$BR(B^0 \rightarrow \rho^+ \rho^-) = (30 \pm 4 \pm 5) \times 10^{-6}$$

$$f_L = 0.99 \pm 0.03^{+0.04}_{-0.03}$$

$$S_{Long} = -0.42 \pm 0.41 \pm 0.14 \quad C_{Long} = -0.17 \pm 0.27 \pm 0.14$$

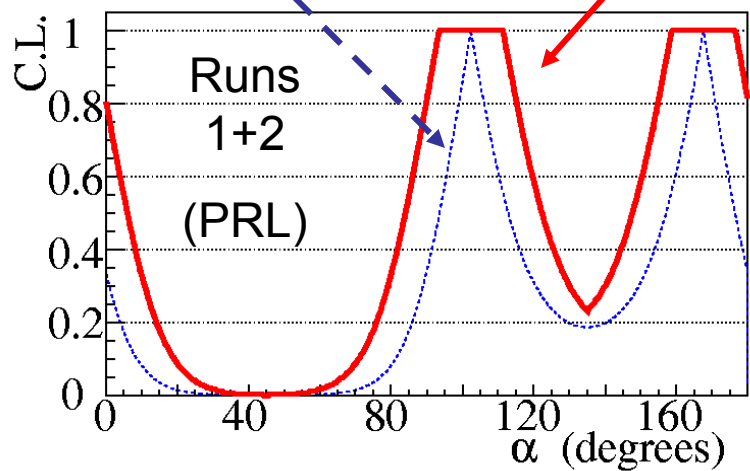
- Runs 1+2+3 (presented at Moriond EW 2004):

$$S_{Long} = -0.19 \pm 0.33 \pm 0.11 \quad C_{Long} = -0.23 \pm 0.24 \pm 0.14$$

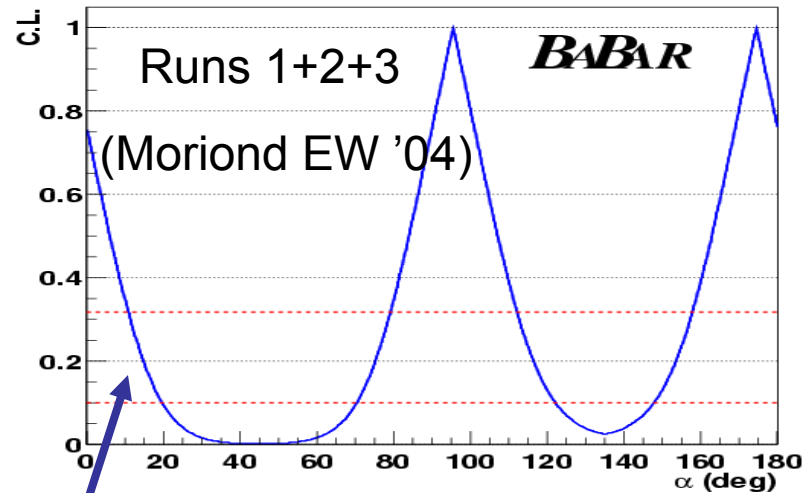
$$\sin^2 \delta \leq \frac{f_{Long}^{00} \times \mathcal{B}(B^0/\bar{B}^0 \rightarrow \rho^0 \rho^0)}{f_{Long}^{+0} \times \mathcal{B}(B^\pm \rightarrow \rho^\pm \rho^0)}$$

Using Grossman Quinn Bound to constrain penguin pollution

α_{eff}



$$\alpha = 102^{\circ} \begin{matrix} +16^{\circ} \\ -12^{\circ} \end{matrix}_{stat} \begin{matrix} +5^{\circ} \\ -4^{\circ} \end{matrix}_{syst} \pm 13^{\circ}_{penguin}$$



$$\alpha = 96^{\circ} \pm 10^{\circ}_{stat} \pm 4^{\circ}_{syst} \pm 13^{\circ}_{penguin}$$

Isospin Analysis

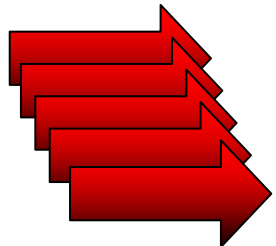
New $\rho^+\rho^-$ Result

- Essentially same method; but there are a few changes
- 210 fb⁻¹ of data used (BaBar's full data set)
- CP fit still uses untagged events to constrain $q\bar{q}$ background shape from data
- new result is an update of S_{Long} , C_{Long} , and f_L
- some improvements in the analysis
 - Δt model for signal is improved
 - better B-background model (updated according to HFAG)
 - interference calculation for systematic errors
- use toy MC to extract CL on α

• Unbinned extended maximum likelihood fit

other modes have similar analysis methodology

- m_{ES} – B mass
- ΔE – energy difference
- Δt – proper time difference
- NN_{out} – neural network
- $m_{\pi\pi}$ (x2) – ρ masses
- $\cos\theta_{hel}$ (x2) – ρ helicity

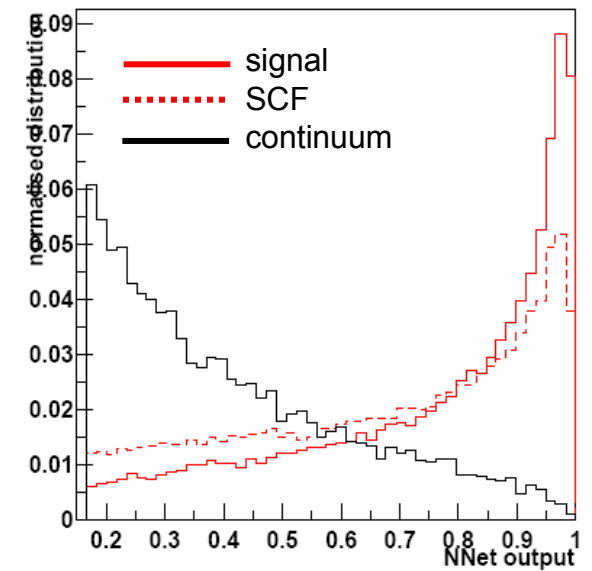


- ### 5 exclusive tagging Categories:
- Leptons
 - High Purity Kaons
 - Lower Purity Kaons
 - Other
 - Un-tagged

NN_{out} : 10 inputs to a multi layer perceptron to discriminate between signal and $e^+e^- \rightarrow$ continuum

$$\left. \begin{aligned} &\sum_{ROE} |p_i^*| \\ &\sum_{ROE} |p_i^*| \cos^2 \theta_i \\ &\sum_{ROE} p_T \end{aligned} \right\} \text{for neutral and charged sums over ROE used separately in MVA}$$

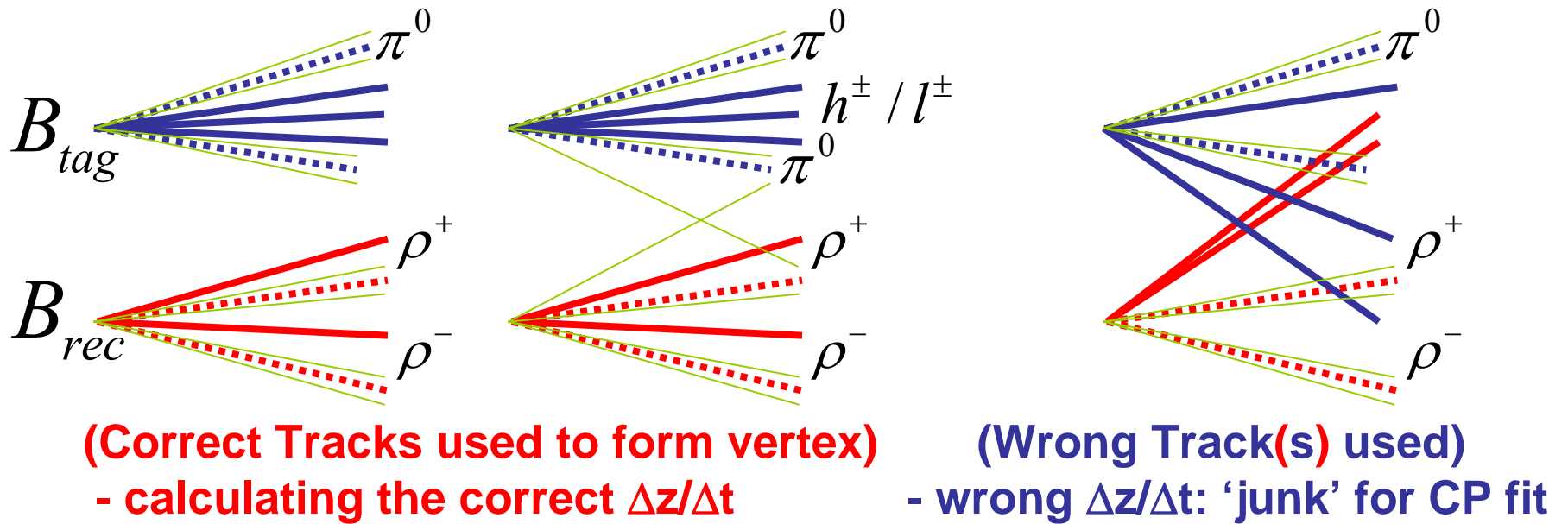
- π^0 decay angle (x2)
- |\cos| of angle between direction of B and Z axis
- |\cos| of angle between the B thrust and Z axis
- |\cos| of angle between the B thrust axis and thrust of ROE



Improvements in Δt model for latest result

Signal is the sum of:

true signal	(51.8%)
correct track SCF	(34.6%)
wrong track SCF	(13.6%)



Wrong track SCF

- pick up one or all tracks from other B meson
- leads to biased S and C for part of the signal

Solution: describe S and C for correct track signal and wrong track signal separately.

$$PDF_{signal} = PDF_{signal}^{long} + PDF_{signal}^{tran}$$

$$PDF_{signal}^{long} = (P_{true}^{long} + P_{correct\ track}^{long}) \times f[S_{Long}, C_{Long}, \Delta t, \sigma_{\Delta t}] \\ + P_{wrong\ track}^{long} \times f[S_{Long}^W, C_{Long}^W, \Delta t, \sigma_{\Delta t}]$$

- Use the correct track signal only for measuring S_{LONG} and C_{LONG}
- Set $S_{Long}^W = C_{Long}^W = 0$ in the fit & apply systematic error for wrong track CP on the final result.
- Benefits of this solution
 - remove bias on CP result due to these events (~1.3° effect).
 - no need for additional systematic errors to cover this.

Brief Summary of Time Dependence of fit

- **split the longitudinal and transverse polarisation**
- **longitudinal signal:**
 - correct track S and C are the S_{Long} and C_{Long} of our result. We use this for α
 - wrong track S and C are set to zero in the nominal fit. Then vary these parameters to ± 1 for systematic errors
- **transverse signal:**
 - do not distinguish between CP odd/even components. Just allow for a common S and C. Vary between ± 1 for systematics
- Correct track events have a common resolution function
- Wrong track events have their own resolution function

Background Summary

In addition to the signal (1% of fit sample)

→ continuum background (92% of fit sample)

→ B background 7% of fit sample)

The **Main** B backgrounds Considered In the fit (38 different modes are included in our background model):

B → charm dominates

$$B^+ \rightarrow \text{charm} = 2551$$

$$B^0 \rightarrow \text{charm} = 1316$$

$$B^+ \rightarrow (a_1\pi)^+ = 87$$

$$B^0 \rightarrow a_1\rho = 145$$

$$B^+ \rightarrow \rho^+\rho^0 = 82$$

$$B^0 \rightarrow a_1\pi = 65$$

$$B^+ \rightarrow a_1\rho^+ = 65$$

$$B^0 \rightarrow K^{**}\pi = 56$$

$$B^+ \rightarrow \rho\pi^0 = 51$$

$$B^0 \rightarrow \rho\pi = 31$$

Final states with charged ρ mesons contribute a lot in our background model.

Fit Results

A total of 26 parameters are floated.

signal yield

S_L, C_L, f_L

22 background parameters

Data sample = 68703 events

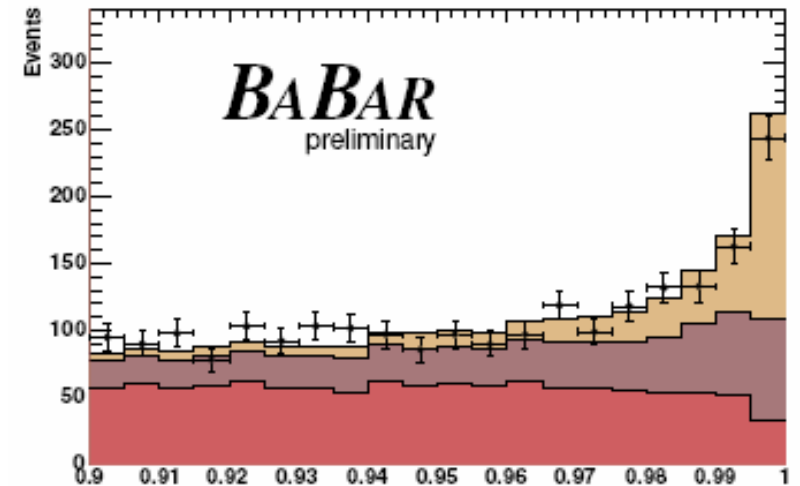
$$N_{signal} = 685 \pm 52 \quad \longrightarrow \quad N_{signal} = 617 \pm 52$$

$$f_L = 0.978 \pm 0.014$$

$$S_L = -0.33 \pm 0.24$$

$$C_L = -0.03 \pm 0.18$$

• compatible with previous results



$$R = \frac{L_{signal}}{L_{signal} + L_{background}}$$

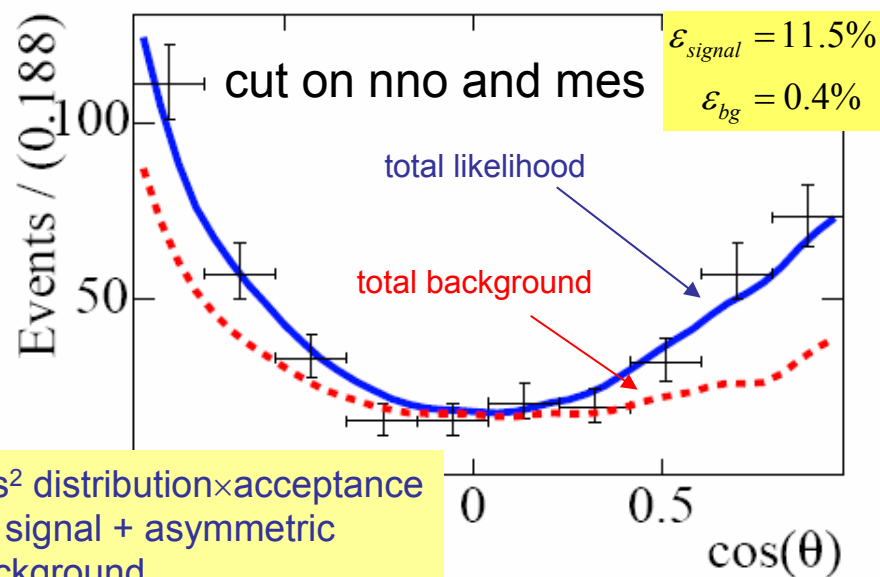
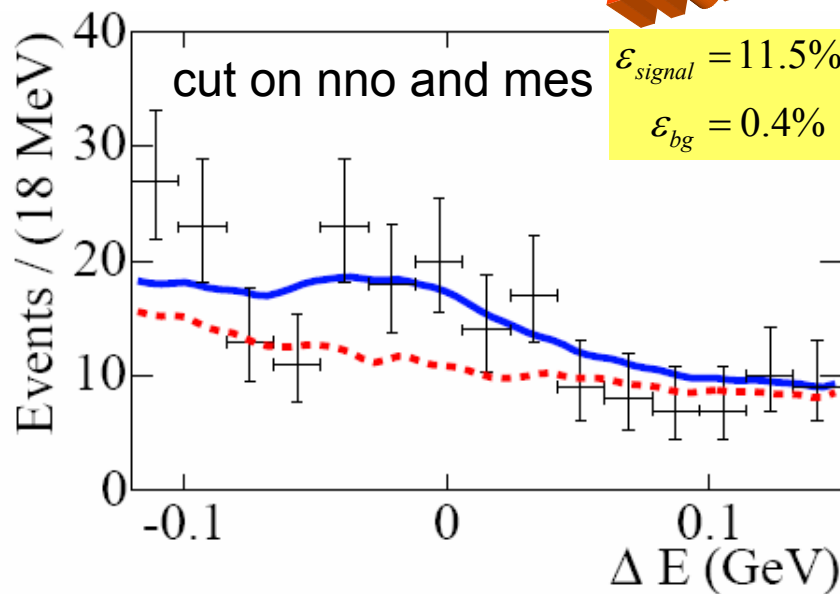
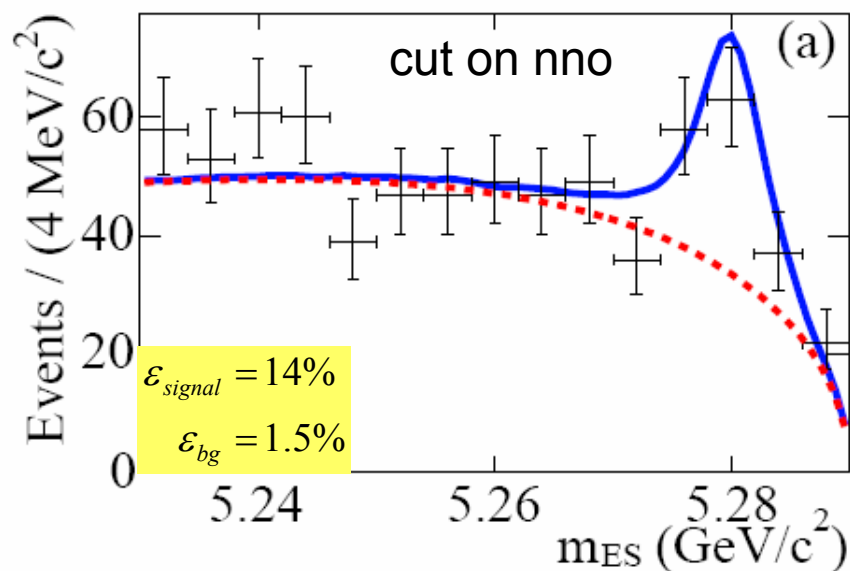
- Correct signal yield for bias coming from correlations that are neglected in the fit model
- These have a small impact on the other parameters (see systematics)



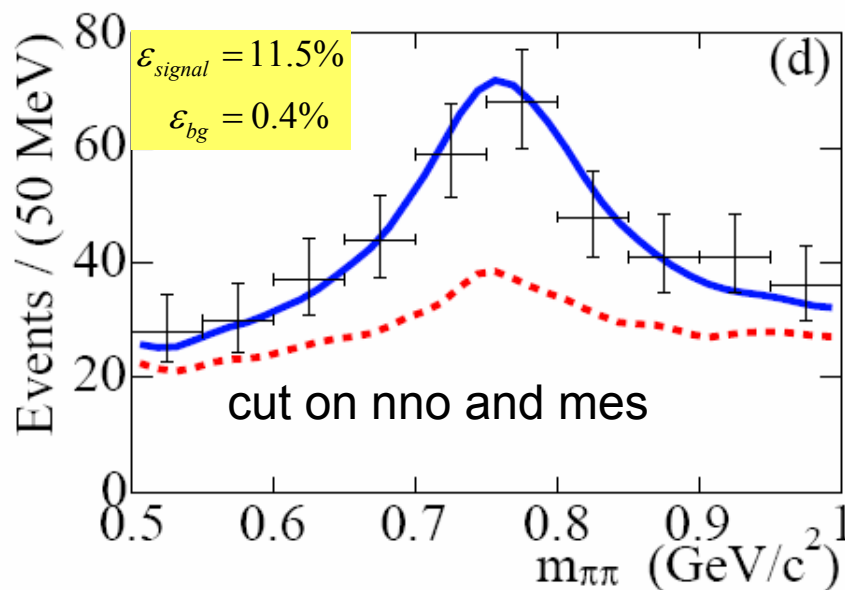
Preliminary

Signal Projection Plots –Lepton and Kaon1 categories only

Preliminary



cos² distribution × acceptance for signal + asymmetric background



Interference calculation (systematic error)

1. Generate toy MC in 5D phase space: $m_1, m_2, \theta_1, \theta_2, \phi$ for $A_{\rho\rho}$ and $A_{\pi\pi}$.
[$\text{xx} = a_1\pi, \rho\pi\pi, \pi\pi\pi\pi$] using BW for resonances
2. Calculate Matrix element including interference term
3. Cut on allowed m_i and θ_i to match $\rho\rho$ selection cuts
4. Calculate effective S and C from toy data: e.g.

$$\lambda(x_i) = \frac{q}{p} \frac{A(\bar{B}^0 \rightarrow \rho^+ \rho^-) + A(\bar{B}^0 \rightarrow a_1^+ \pi^-) + A(\bar{B}^0 \rightarrow a_1^- \pi^+)}{A(B^0 \rightarrow \rho^+ \rho^-) + A(B^0 \rightarrow a_1^+ \pi^-) + A(B^0 \rightarrow a_1^- \pi^+)} \Rightarrow S(x_i) = \frac{2 \text{Im}(\lambda(x_i))}{1 - |\lambda(x_i)|^2}$$

$$S^{\text{eff}}(x_i) = \frac{\int S(x_i) \left| A(\bar{B}^0 / B^0 \rightarrow a_1^+ \pi^-) \right|^2 d^5 x_i}{\int \left| A(\bar{B}^0 / B^0 \rightarrow a_1^+ \pi^-) \right|^2 d^5 x_i}$$

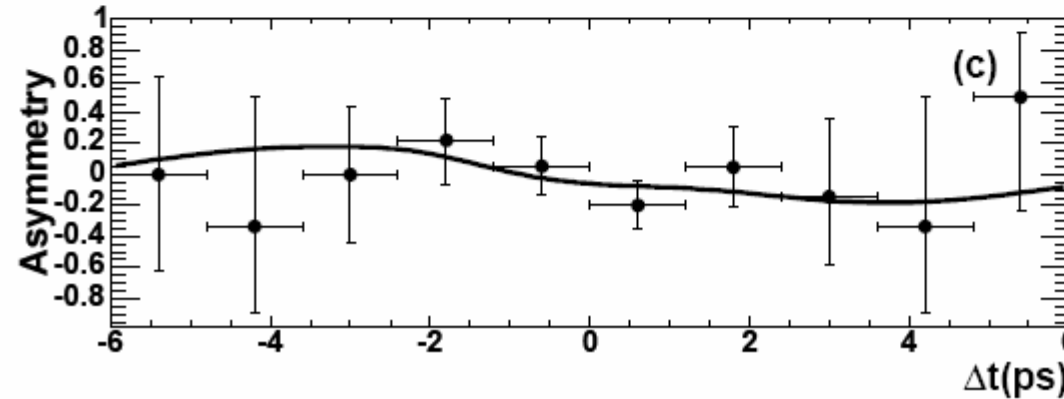
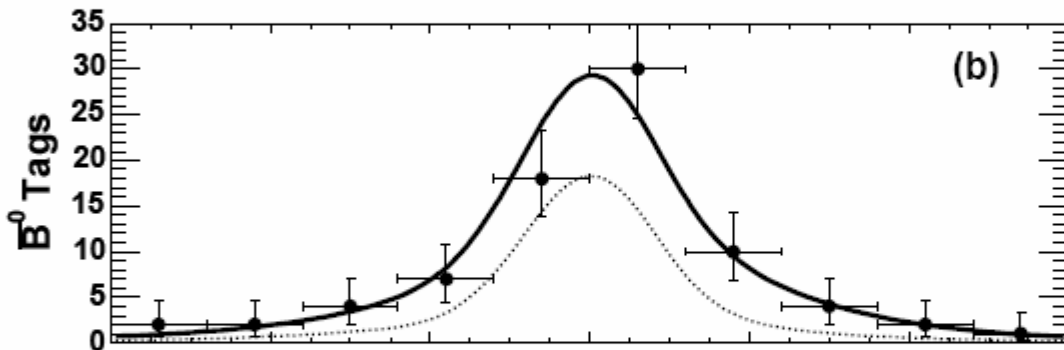
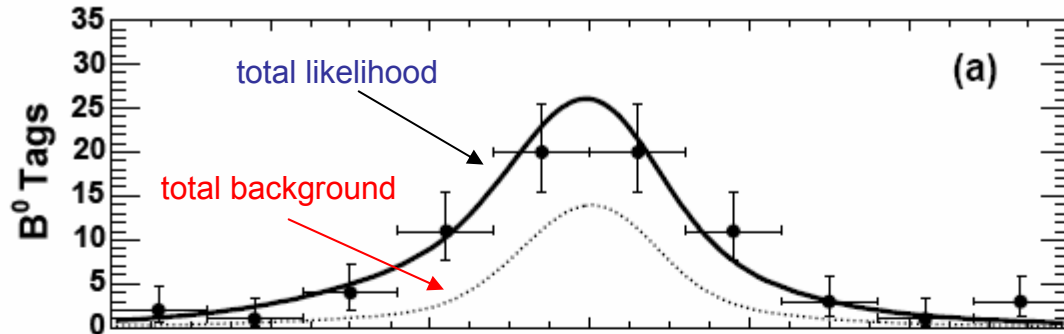
5. Take the RMS deviation of $O_{\text{eff}} - O$ as the systematic error.

- also looked at $\sigma(400)\pi\pi$, but ignored this final state as it has a small efficiency relative to the other final states included here.

Total Systematic Uncertainty

Contribution	f_L	S_{long}	C_{long}
B -background yield	± 0.003	± 0.027	$+0.002$ -0.003
B -background CP	± 0.001	± 0.027	± 0.045
non-resonant events	0.015	0.030	0.001
Floating B - background	-0.020	-0.12	+ 0.008
Neglecting Interference	0.0036	0.023	0.022
DCSD	–	0.012	0.037
SVT LA (alignment)	–	0.034	0.005
Fit bias	0.010	0.04	0.05
CPV in wrong track SXF	0.0005	$+0.007$ -0.002	± 0.012
.			
.			
.			
Total	$+0.021$ -0.029	$+0.08$ -0.14	± 0.09

Table 1: Summary of the main systematic errors contribution to f_L , S_{long} and C_{long}



Events from the
Lepton and
Kaon1 tagging
categories only.

$$S_{Long} = -0.33 \pm 0.24^{+0.08}_{-0.14}$$

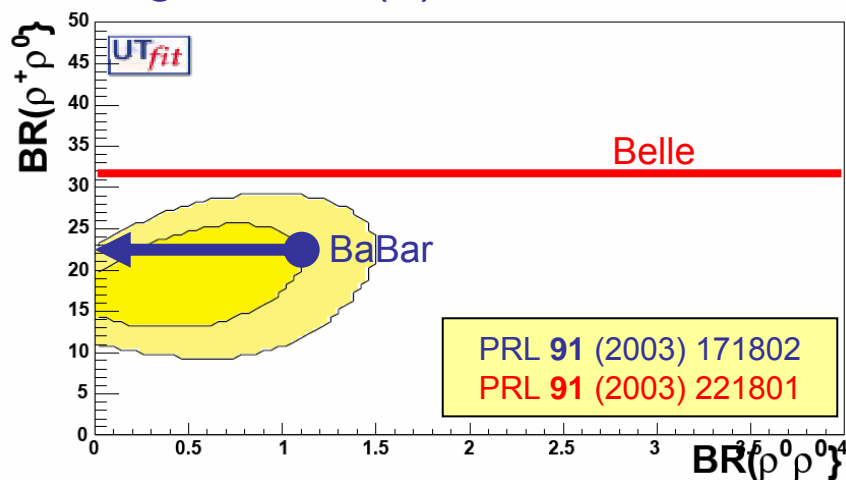
$$C_{Long} = -0.03 \pm 0.18 \pm 0.09$$

$$f_L = 0.978 \pm 0.014^{+0.020}_{-0.028}$$

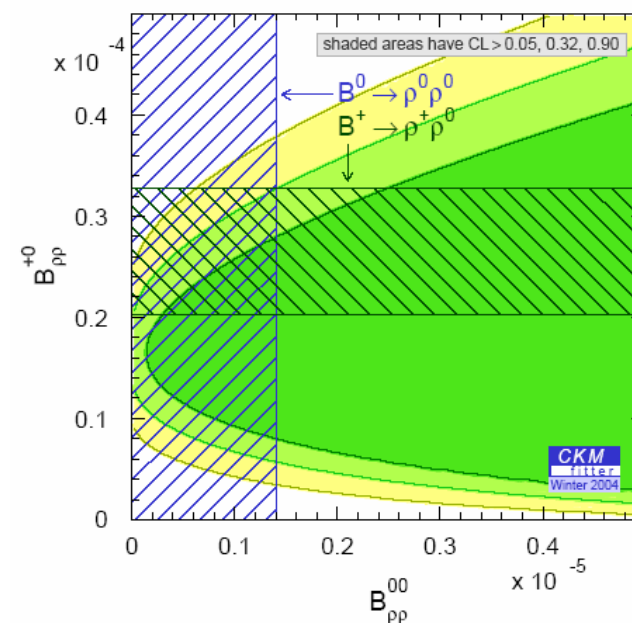
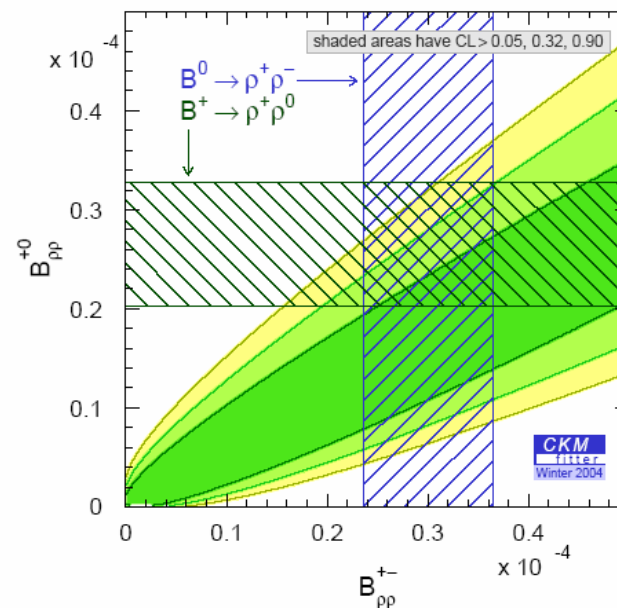
Preliminary

$B \rightarrow \rho^+ \rho^0$

➔ UT Fit and CKM Fitter predict that the central value of $BF(B^+ \rightarrow \rho^+ \rho^0)$ is a little too large for SU(2).



➔ An updated measurement of this mode is long overdue & we're eagerly awaiting it!



Measuring α

➔ Use Isospin analysis for longitudinal polarisation

$B^0 \rightarrow \rho^+ \rho^-$ (BaBar)

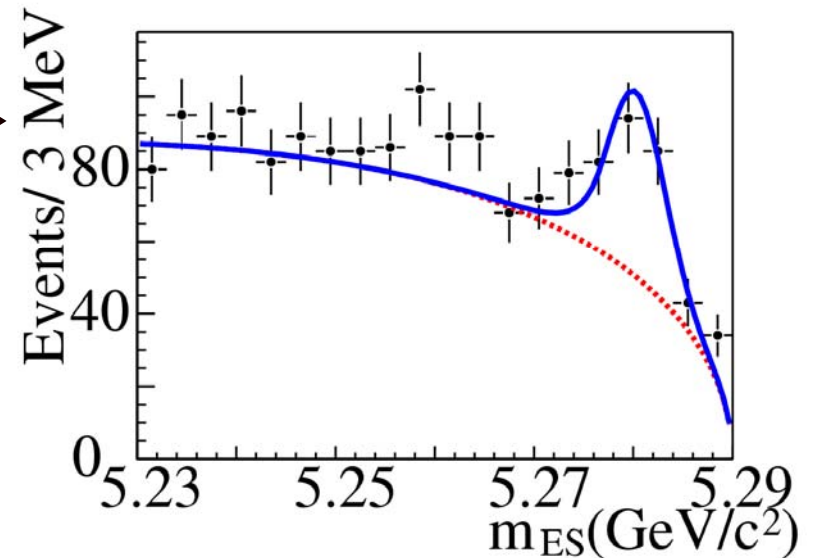
PRL **93** 231801
(2004)

$$BF = (30 \pm 4 \pm 5) \times 10^{-6}$$

(88e6 B Pairs)

new $f_L = 0.978 \pm 0.014^{+0.021}_{-0.028}$

(230e6 B Pairs)



$B^+ \rightarrow \rho^+ \rho^0$ (Belle & BaBar)

$$BF = (26.4 \pm 6.4) \times 10^{-6}$$

$$f_L = 0.96^{+0.05}_{-0.07}$$

PRL **91** (2003) 171802
PRL **91** (2003) 221801

$B^0 \rightarrow \rho^0 \rho^0$ (BaBar)

$$BF < 1.1 \times 10^{-6} \text{ (90\% C.L.)}$$

hep-ex/0412067 (227e6 B Pairs)

Penguins are small in $B \rightarrow \rho\rho$
 $|\alpha_{eff} - \alpha| < 11^\circ \text{ (68\% CL)}$

- Build a χ^2_{\min} from the measured observables (S,C, f_L and BR) each of which can be related to the amplitudes that make up the isospin triangles.

$$\chi^2 \text{ scan in } \alpha \quad \Delta\chi^2(\alpha) = \chi^2_{\min}(\alpha) - \chi^2_{\min 0}$$

To obtain the CL: we use toy MC to reproduce what happens with data: i) Generate toy for each alpha scanned

ii) calculate $1 - \text{CL}(\alpha)$: fraction of toys with

$$\Delta\chi^2(\alpha)_{\text{toy}} > \Delta\chi^2(\alpha)_{\text{data}}$$

Toy MC techniques work better in this case as the isospin triangle is not closed (so is unphysical):

$$1 / \sqrt{2} \left| A_{Long}^{+-} \right| + \left| A_{Long}^{00} \right| \leq \left| A_{Long}^{+0} \right|$$

Assumptions in the use of SU(2) with $\rho^+\rho^-$

- ➔ Assume Gronau-London Isospin analysis
(use SU2 without electroweak penguins)
- ➔ Neglect I=1 component of amplitude
(should be $O(\Gamma_\rho/m_\rho)^2 \approx 4\%$) Falk et al, PRD 69 011502 (2004)
- ➔ (implicitly we also neglect higher ρ resonances
in the final state when extracting S and C)

The α Result

$$S_{Long} = -0.33 \pm 0.24^{+0.08}_{-0.14}$$

$$C_{Long} = -0.03 \pm 0.18 \pm 0.09$$

$$f_L = 0.978 \pm 0.014^{+0.020}_{-0.028}$$

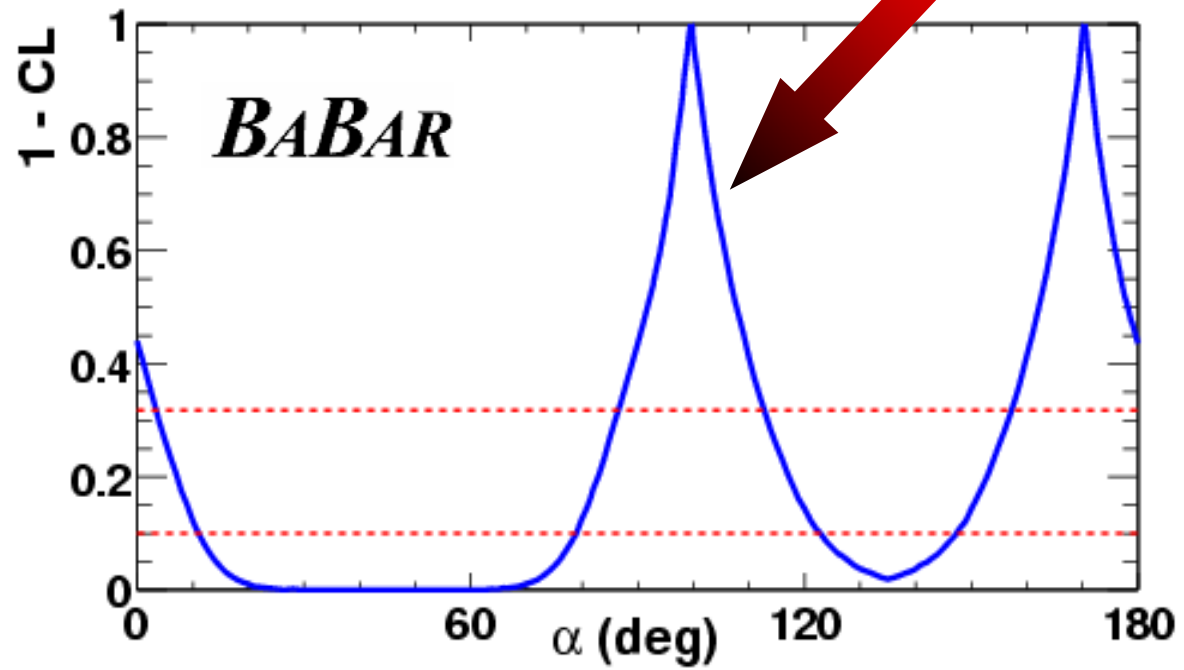
Inputs from other $\rho\rho$ measurements

$$\alpha \in [79^\circ, 123^\circ] \text{ at } 90\%CL$$

Neglect:

- EW penguins (1-2° effect (CKM Fitter/Gronau & Zupan))
- Possible I=1 amplitudes

Penguin error is $\pm 11^\circ$ at 1σ .



The solution in agreement with the SM is:

$$\alpha = 100^\circ \pm 13^\circ$$

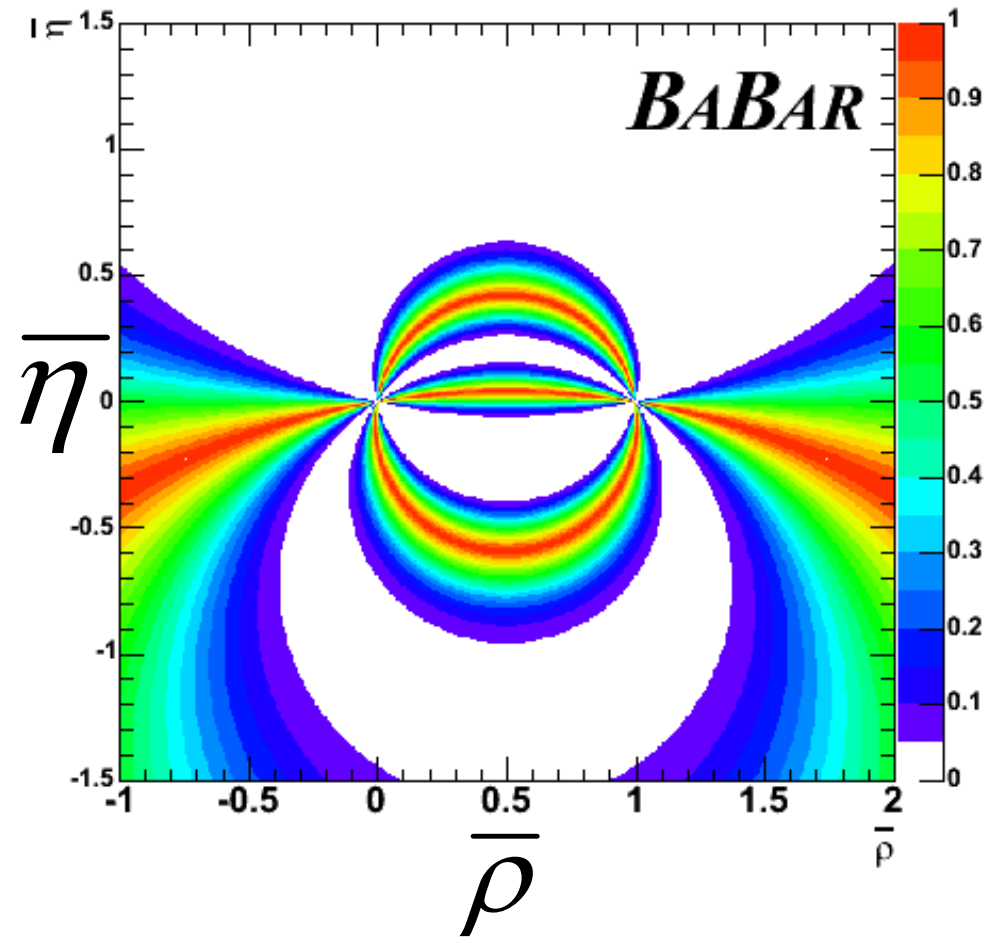
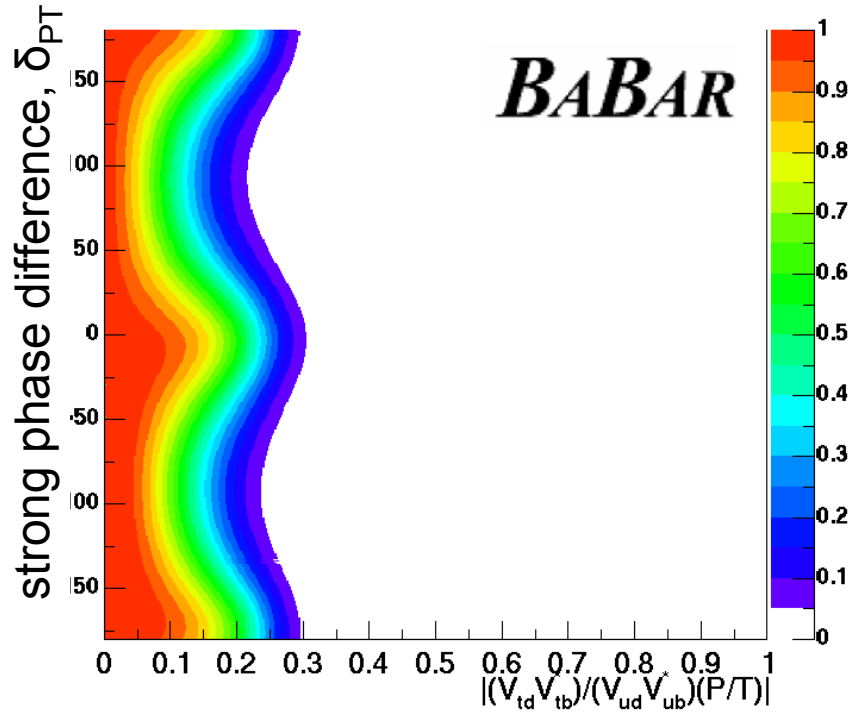
Preliminary

- Using these results, we can constrain $|P/T|$ in $\rho\rho$
- and also show the α constrain in the $\bar{\eta}\bar{\rho}$ plane.

Preliminary

$$P = P_t - P_c$$

$$T = T + P_u - P_c$$



$$|P/T| = 0.07^{+0.14}_{-0.07}$$

(same P, T convention as CKM Fitter for the $|P/T|$ plot)

Summary

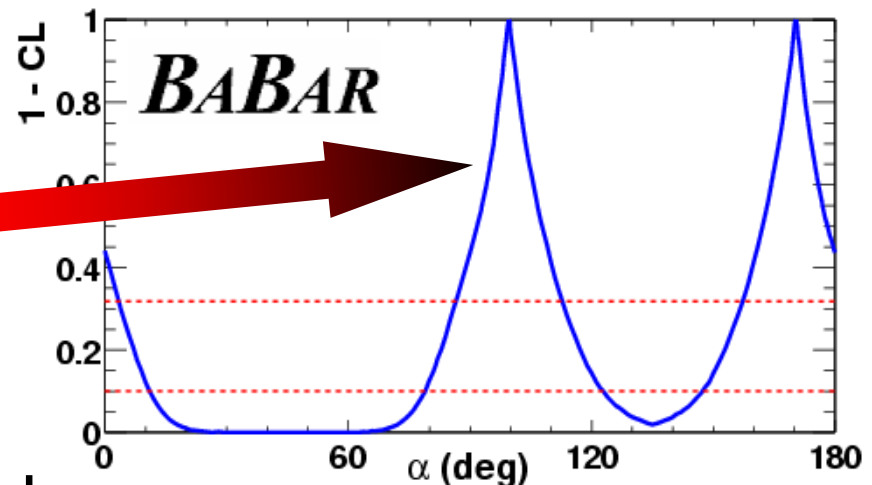
- New result on $\rho^0\rho^0$ last summer
- New result this winter for $\rho^+\rho^-$

→ updated CP + f_L measurement

$$S_{Long} = -0.33 \pm 0.24^{+0.08}_{-0.14} \quad C_{Long} = -0.03 \pm 0.18 \pm 0.09$$
$$f_L = 0.978 \pm 0.014^{+0.021}_{-0.029}$$

- Updated Isospin analysis result

$$\alpha = 100^\circ \pm 13^\circ$$



- need to see $\rho^+\rho^0$ updated soon.